

Evaluation of General Correlations for Heat Transfer During Boiling of Saturated Liquids in Tubes and Annuli

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ABSTRACT

Six of the most verified correlations for boiling heat transfer were compared to data for horizontal and vertical tubes and annuli. The correlations evaluated were: Chen (1966), Shah (1982), Gungor and Winterton (1986), Liu & Winterton (1991), Kandlikar (1990), and Steiner and Taborek (1992). The database used to evaluate these correlations included 29 fluids: water, refrigerants, cryogenics, organic and inorganic chemicals. The data cover reduced pressures from 0.005 to 0.783, mass flux from 28 to 11071 kg/m²s, vapor quality from 0 to 0.95, and boiling number from 0.000026 to 0.00742. The correlations of Shah and Gungor & Winterton gave the best agreement with data with a mean deviation of about 17.5%, only a couple of data sets showing large deviations. The paper presents and discusses the results of this study. Included are tables giving the range of dimensional and non-dimensional parameters covered by each experimental study.

Keywords: boiling, heat transfer, evaporation, tubes, correlations

INTRODUCTION

Hundreds of correlations have been proposed for the calculation of heat transfer during boiling of saturated liquids inside tubes and annuli. Most of them have been compared to only a limited amount of data. However, some of them have been shown to agree with a wide range of data with many fluids and are therefore considered as general correlations. It is desirable to know their comparative accuracy and limitations so that the most reliable ones may be used for practical calculations. This paper reports the results of such a study in which six of the best known general correlations were compared to a very wide range of data for 29 fluids. Included are tables giving the range of dimensional and non-dimensional parameters covered by each experimental study.

NOMENCLATURE

Bo	Boiling number = $q/(G h_{fg})$
D	ID of tube
D _{hp}	Equivalent diameter of annulus
Co	Convection number, = $(1/x - 1)^{0.8} (\rho_g / \rho_L)^{0.5}$
F _{chen}	Convective enhancement factor in Chen correlation
F _{ST}	Convective enhancement factor in Steiner & Taborek correlation
Fr _L	Froude number, = $G^2 / (\rho_L^2 gD)$
G	Total mass flux (liquid plus vapor)
G	Acceleration due to gravity
h _{fg}	Latent heat of vaporization
h _{LO}	Heat transfer coefficient assuming liquid phase flowing alone
h _{LT}	Heat transfer coefficient assuming all mass flowing as liquid
h _{meas}	Measured heat transfer coefficient
h _{pb}	Pool boiling heat transfer coefficient
h _{pred}	Predicted heat transfer coefficient
h _{TP}	Two-phase heat transfer coefficient
k	Thermal conductivity of liquid
Pr	Prandtl number of liquid
p _r	Reduced pressure
q	Heat flux
S	Nucleate boiling suppression factor in Chen correlation

Greek

μ	Viscosity of liquid
ρ _L	Density of liquid
ρ _g	Density of vapor

AVAILABLE CORRELATIONS

A very large number of correlations have been published. Most of them have had very little verification. Only the ones that have had extensive verification with a wide range of fluids and have found wide acceptance are mentioned here.

The first general correlation was published by Chen [1]. It was based entirely on data for vertical channels. The correlation is:

$$h_{TP} = F_{chen} h_{LO} + Sh_{pb} \quad (1)$$

It showed excellent agreement with the data analyzed by Chen. However, many later researchers compared it to large data bases and reported that its agreement was not satisfactory either with horizontal or vertical channels. Examples of such studies are Kandlikar [2], Gungor and Winterton [3], Liu and Winterton [4], Gungor and Winterton [5], and Steiner & Taborek [6].

Hundreds of correlations of the form of Eq. (1) have been proposed, most of them based only on one data set.

The present author, Shah [7, 8], presented a correlation whose functional form is:

$$h_{TP} / h_{LO} = f(Co, Bo, Fr_L) \quad (2)$$

The Froude number Fr_L accounts for stratification in horizontal channels; it is not used for vertical channels. The correlation is given in the Appendix. This was the first correlation applicable to both horizontal and vertical tubes. It has been tested with large databases by many researchers [2, 3, 4, 5] with mostly satisfactory results.

Kandlikar [2] has given a correlation applicable to both horizontal and vertical channels. It uses the same correlating parameters as the Shah correlation but also has a fluid specific multiplier for nucleate boiling. Values of this multiplier have been given only for 10 fluids. Hence it is applicable to only those 10 fluids.

Gungor and Winterton [3] presented a correlation similar to Eq. (1) but incorporated the Froude number for horizontal channels in the same way as in the Shah correlation. Liu and Winterton [4] also presented a similar correlation and showed it to be more accurate than the Gungor and Winterton correlation [3].

Gungor and Winterton [5] presented a correlation similar to the Shah correlation and showed it to agree with a wide range of data.

Steiner and Taborek (6) have given a correlation which is based on a large and varied database for vertical channels. It has the form:

$$h_{TP} = \left((F_{st} h_{LT})^3 + h_{pb}^3 \right)^{1/3} \quad (3)$$

CORRELATIONS TESTED

The following correlations were tested:

Chen [1] with pool boiling component calculated by the Cooper correlation [9]; Steiner and Taborek [6]; Shah [8]; Kandlikar [2]; Liu and Winterton [4]; Gungor & Winterton [5].

The reason for using the Cooper pool boiling correlation with the Chen correlation is that the Cooper correlation has been verified with an extremely wide range of data while the pool boiling correlation originally used by Chen has had very little verification. It was felt that this change will improve the accuracy of the Chen correlation. Henceforth, the Chen correlation with this change is called the Chen-Cooper correlation. Note that the Cooper correlation has been used without the factor 1.7 for copper tubes which Cooper stated to be a possibility and assuming tube roughness to be 1 μm .

The Gungor & Winterton correlation [3] was not tested as Liu & Winterton (4) has been tested and they showed that their correlation gave better agreement with data.

All of the above correlations require the calculation of single-phase liquid heat transfer coefficient. For use with the Steiner and Taborek correlation, the formula of Pethukov and Krillov [10] was used in accordance with their recommendation. For all other tested correlations, liquid convective heat transfer was calculated by the McAdams equation [12]:

$$\frac{h_{LT} D}{k} = 0.023 \left(\frac{GD}{\mu} \right)^{0.8} \text{Pr}^{0.4} \quad (4)$$

Ogata and Sato [17] had compared their non-boiling helium data with Eq.(4) and found that the constant should be changed to 0.015 to fit their data. Therefore in analyzing their data, the constant in Eq. (4) was changed to 0.015. For application to annuli, D was replaced by the equivalent diameter D_{hp} defined as four times the flow area divided by the heated perimeter.

DATA ANALYZED

Efforts were made to collect data for as many fluids as possible covering a wide range of parameters. Only single component fluids and azeotropic mixtures were considered. For refrigerants, only those data were considered for which oil content was stated to be zero or negligible.

The salient features and range of data analyzed are listed in Tables 1 and 2. These include 28 fluids, namely: water, R-11, R-12, R-22, R-32, R-113, R-114, R-123, R-134a, R-152a, R-502, ammonia, propane, isobutane, carbon tetrachloride, isopropyl alcohol, ethanol, methanol, n-butanol, cyclohexane, benzene, heptane, pentane, nitrogen, argon, neon, hydrogen, nitrogen, and helium. Data for carbon dioxide from several sources were also analyzed but none of them agreed with any of the tested correlations. It was concluded that carbon dioxide is a special fluid requiring separate treatment. Hence CO_2 data were not included in Tables 1 and 2. This is further discussed later in the paper.

Most of the data analyzed are for local heat transfer coefficients. Some researchers have reported only the average heat transfer coefficients and heat flux over the tube length as indicated in Tables 1 and 2. Comparison with such data was done by using the mean quality and the mean heat flux in the evaluated correlations.

The data of Ogata and Sato [17] for helium showed strong hysteresis. The mean of the heat transfer coefficients for ascending and descending heat fluxes were used for comparison with all correlations.

FLUID PROPERTY DATA

The main source of fluid property data was the University of Ottawa Code UO0694. It did not give data for all fluids. For analyzing the data of Talty [13], fluid properties used were those listed by him. For helium, properties used were from McCarty [14]. Properties of iso-butane, propane, ammonia, R-32, R-502, hydrogen, argon, and Neon were from ASHRAE Handbook [15]. Properties of other fluids (carbon tetrachloride, n-butanol), were from Beaton and Hewitt [16]

RESULTS OF DATA ANALYSIS

The mean and average deviations of data from correlations are listed in Tables 1 and 2 for horizontal and vertical channels respectively. The deviation for a data point is defined as:

$$\delta = \frac{(h_{pred} - h_{meas})}{h_{meas}} \quad (5)$$

The average deviation δ_{avg} of a data set is defined as:

$$\delta_{avg} = \Sigma(\delta) / N \quad (6)$$

where N is the number of data points in the data sets. The mean deviation δ_{mean} of a data set is defined as:

$$\delta_{mean} = \Sigma Abs.(\delta) / N \quad (7)$$

Table 3 gives the combined results for horizontal and vertical channels. In this table, the deviations for each correlation are given in two ways:

1. Giving equal weight to each data point.
2. Giving equal weight to each data set.

The second way probably gives a better indication of the reliability of the correlation.

DISCUSSION OF RESULTS

Accuracy of Correlations

It is apparent from the results in Tables 1, 2, and 3 that the correlations of Shah [8] and Gungor & Winterton [5] are the most reliable with a mean deviation of about 17.5% for all 1859 data points. The Shah correlation is more consistent as only 5 of the 67 data sets have deviation more than 30% while the Gungor & Winterton correlation has 9 data sets exceeding 30% mean deviation.

The correlations of Shah and Gungor & Winterton show reasonable agreement with almost all data sets. One notable exception is the data of Mohr and Runge [18] for neon. These are much higher than all the correlations tested here. No other analyzable data for neon could be found. However, Pappel and Hendricks [19] gave a correlation of their subcooled data for nitrogen and neon for subcooling starting from 2 degree C. The predictions of this correlation at 1 degree subcooled neon agree satisfactorily with the Shah correlation and are lower than the Shah correlation at 2 degree subcooling. This suggests that the Mohr and Runge data may be unusually high.

The other notable exception is the data of Steiner and Schlunder [20] for nitrogen; these are much higher than the Shah correlation. However, nitrogen data from three other

sources [19, 21, 22] agree well with this correlation. The Steiner & Schlunder data are also much higher than the Gungor-Winterton and Liu-Winterton correlations. Hence these data are apparently unique.

The Liu-Winterton correlation's performance is erratic. While it agrees well with many data sets, it shows large deviations with many data sets, for example the data of Muller for Argon [23], cyclohexane data of Talty [13], data of Piret and Isbin [24] for water, CCl₄, n-butanol, and iso-propanol.

The Steiner and Taborek correlation did not perform well in predicting horizontal tube data. Indeed these authors have recommended it only for vertical channels. Even with vertical channels, it shows large deviations with some data sets.

The Chen-Cooper correlation works fairly well with both horizontal and vertical tubes but its accuracy is significantly less than the correlations of Shah and Gungor-Winterton.

The Kandlikar correlation could be compared with data for only those fluids for which he gave the nucleate boiling multiplying factors. Even among those fluids, it performed poorly with data for R-22, nitrogen, and neon. If the data for these three fluids are deleted, the mean deviation of Kandlikar correlation becomes 16.8% instead of 32.2% if data for these three fluids are included. The apparent reason is that the nucleate boiling multiplying factors for these fluids were determined by Kandlikar from abnormally high data. Those data might have been high because of the surfaces of those test sections having unusually favorable microstructure as discussed later in this paper. The effect of Kandlikar's multiplying factor is highest at zero vapor quality; hence the +436% deviation with the nitrogen data of Pappel and Hendricks which is at zero vapor quality, the multiplying factor for nitrogen being 4.7 (it is 1 for water).

Tube Material

The data analyzed include many types of tube materials including copper, stainless steel, monel, brass, and nickel-coated glass. All the test sections were made from commercial grade tubes except the nickel-coated glass used by Gouse and Coumou [32]. There is no indication that the accuracy of the correlations is affected by the type of material.

Tube Surface Characteristics

It is generally accepted that the intensity of nucleate boiling depends on the shape and population densities of cavities in the surface. This has been demonstrated by pool boiling tests on surfaces with artificially made cavities. Information on cavity size and cavity population density is not available for any of the test data evaluated here. The fact that almost all data sets are in reasonable agreement with the correlations of Shah and Gungor & Winterton (which do not have any factor for surface microstructure) indicates that the variations in microstructures of commercial tubes are normally small. It may be noted that the most successful general pool boiling correlations (Cooper [9], Stephan and Abdelsalam [62]) do not have any factor for surface microstructure. It is possible that some commercial tubes may have a microstructure very favorable to nucleate boiling. This may be the explanation for the data of Steiner & Schlunder and Mohr and Runge being much higher than predictions of almost all tested correlations.

It should be noted that the designer of heat exchanger has no way of knowing the microstructure of the tubes that will be used in fabrication. It is therefore fortunate that heat transfer

coefficients can be predicted with a high probability of accuracy without the knowledge of microstructure.

Heating Mode

The data analyzed include electric heating, heating by condensing steam, and heating by hot liquids. Data for all heating modes are satisfactorily correlated by the correlations of Shah and Gungor & Winterton.

Type of Fluid

The Shah and Gungor-Winterton correlations show good agreement with 28 of the 29 fluids included in Tables 1 and 2. The only available single data set for neon does not agree with any of the tested correlations but as was pointed out earlier, the measurements of Pappel and Hendricks [19] appear to be in agreement with the Shah correlation.

CO₂ data from several sources were analyzed but none of the correlations tested here was found to agree with them. Among such data are those of Bredsen et al [59], Yoon et al. [60] and Knudsen and Jensen [61]. These authors also compared their data with well-known general correlations with poor results. Thome and Hejal [26] compared carbon dioxide data from six sources with their correlation which was based on data for several refrigerants but found poor agreement. They concluded that carbon dioxide is a unique fluid and developed a correlation specifically for CO₂.

Thus the correlations of Shah and Gungor & Winterton appear to be suitable for all Newtonian, non-metallic fluids except carbon dioxide

Variation of Heat Transfer With Vapor Quality

For correct design of an evaporator, it is important that a correlation correctly predict variation with quality. All the authors of the correlation tested have shown by comparison with data, in the papers presenting those correlations, that they predict the correct trend. Kandlikar [63] showed that his correlation agrees with the data of Jallouk [64] in vertical tube which show decreasing heat transfer with increasing quality. Shah [8] showed that his correlation predicts decreasing heat transfer with increasing quality at higher Bo and/or higher reduced pressures.

During the present data analysis it was seen that in most cases low mean deviation with a data set was accompanied by correct prediction of the variation of heat transfer with quality.

SUMMARY AND CONCLUSION

1. Six of the best known general correlations were tested with data for 29 fluids including water, refrigerants, organics, and cryogenics boiling in horizontal and vertical tubes and annuli. The data covered a very wide range of parameters.

2. The correlations of Shah [8] and Gungor & Winterton [5] gave good agreement with data, mean deviation being about 17.5%. The Shah correlation was somewhat more consistent. The range of data satisfactorily predicted is given in Table 4. The other four correlations had mean deviations from 22 to 46%.

3. The results indicate that the correlations of Shah and Gungor & Winterton can be used with confidence with all Newtonian non-metallic fluids (except CO₂).

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Table 1: Results of comparison of data for horizontal tubes with various correlations..

Data of	Dia. mm	Material (Heating By)	Fluid	Pr	G Kg/m ² s	q kW/m ²	x, %	Bo 10 ⁴	Co	Fr	No. of data	Deviation, %					Mean Average
												Shah 1982	G-W	L-W	Kandlikar	S-T	
Mumm [45]	11.8	SS (Electr.)	Water	0.014	345	157	0.00	0.53	0.04	1.1	184	11.4	10.9	13.2	13.3	31.8	32.2
				0.0624	1382	788	52.0	11.0	1000	20.0	-5.6	-0.2	-6.1	-10.1	-31.1	-30.9	
Chawla [29]	6.0	Copper (Electr.)	R-11	0.0135	40	2.3	10.0	2.0	0.02	0.025	57	14.8	19.9	28.3	13.9	36.1	21.2
					252	69.9	90.0	26.7	0.28	0.46	-14.8	-15.1	-28.3	-7.6	-34.1	-20.7	
Haynes & Fletcher [34]	1.95	Copper (Elect.)	R-11	0.0135	25	1.2	10.0	0.51	0.01	0.002	29	11.7	14.6	19.0	12.0	58.7	30.0
					130	23.3	90.0	24.3	0.28	0.045	8.2	-4.7	-3.4	10.9	51.4	24.7	
Wattalet et al. [55]	7.0	Copper (Electr.)	R-12	0.0089	22	1.8	10	1.3	0.01	8E-4	52	18.8	12.5	17.3	17.9	105.4	54.8
				0.0198	74	11.6	90	28.0	0.34	0.099	15.8	1.2	-0.9	13.2	103.6	54.8	
Uchida et al. [54]	6.4	SS (Electr.)	R-12	0.0987	150	53.0	0.00	7.75	0.46	0.63	6	27.0	13.2	35.3	19.2	73.8	25.1
				0.1098	420	17.0	17.0	21.7	1000	4.93	-23.1	-5.2	-35.3	10.6	-73.8	-25.1	
Chaddock & Noerager, [28]*	11.7	SS (Elect.)	R-12	0.088	50	2.0	10.0	1.1	0.01	0.019	50	12.9	15.5	16.2	11.8	20.2	8.5
				0.086	300	20.0	92.0	6.7	0.72	0.62	-12.3	-12.8	-10.4	-2.7	2.4	-3.7	
Ebisu, & Torikoshi [31]	6.4	Copper (Liquid)	R-22	0.097	345	14.4	0.00	1.9	0.01	0.25	40	16.3	20.8	15.6	15.7	18.3	18.3
				0.1098	518	27.9	95.0	5.7	1000	2.5	-21.5	-11.7	=10.4	-19.2	-18.1		
Mather [45]	9.5	Copper (Electr.)	R-22	0.11	300	7.5	20.0	1.2	0.04	0.88	4	20.2	22.5	17.5	20.6	12.2	16.5
				0.097	146	7.7	3.0	2.5	0.03	0.14	17.1	18.4	18.4	48.0	22.7	16.9	
Johnston & Chaddock, [36]*	11.6	Copper (Electr.)	R-22	0.16	877	40.5	80.0	6.8	2.7	5.8	69	-8.7	-2.8	3.4	43.5	1.3	-10.4
				0.0134	15	1.7	9.7	3.2	0.09	0.0016	13.8	21.4	50.1	86.3	18.5	25.9	
Muzzio et al. [47]*	8.9	Copper (Liquid)	R-22	0.0581	571	21.5	38.5	13.3	0.28	0.0147	22	-1.7	-20.4	-50.1	86.3	-15.4	25.3
				0.117	90	5.2	0.45	2.9	0.16	0.058	26.7	17.8	17.6	9.1	10.9	19.6	
Pierre [49]*	18.0	Copper (Liquid)	R-22	0.071	400	24.0	0.45	3.0	0.13	1.14	6	-26.7	-10.4	-10.4	9.1	-7.4	-16.5
				0.049	178	11.7	0.55	4.4	0.08	0.082	8.2	11.6	22.3	41.7	34.2	2.3	
Jung et al. [37, 38]	9.0	Copper (Electr.)	R-22	0.081	516	44.0	70.0	4.1	0.66	1.8	12	-12.7	-8.9	-10.5	33.0	-2.7	-18.3
				0.08	367	17.0	5.0	1.5	0.06	2.1	7.8	14.7	14.4	12.5	29.9	5.6	
			R-114	0.081	362	10.0	12.0	1.5	0.05	0.69	20	3.4	10.4	13.7	10.7	29.9	-4.8
			R-152a	0.08	367	17.0	5.0	1.5	0.06	2.1	19	9.7	13.0	60.2	9.3	35.9	10.4
					36.2	36.2	68.0	4.0	0.44	0.44		-9.7	-3.6	60.2	-7.0	35.9	-9.7

Data of	Dia. mm	Material (Heating By)	Fluid	Pr	G Kg/m ² s	q kW/m ²	x, %	Bo 10 ⁴	Co	Fr	No. of data	Deviation, %				Mean Average	
												Shah 1982	G-W	L-W	Kandlikar	S-T	Chen-Cooper
Reid et al. [50]	8.7	(Electr.)	R-113	0.117	248	18.4	3.0	5.8	0.06	0.362	9	19.9	13.5	14.5	9.9	25.7	18.4
Shin et al. [52]	7.7	SS (Electr.)	R-22	0.145	424	18	10	0.69	0.05	1.54	35	19.5	-11.4	-9.9	8.8	-24.1	-18.4
			R-32	0.20	742	30	79	3.64	0.91	4.74	8.5	13.4	12.7	51.5	50.9	17.9	6.5
Gouse & Coumo [32]	10.9	Glass, Ni-coated (electr.)	R-134a	0.109	424	30.0	5.0	1.7	0.18	2.3	12	9.6	9.0	13.6	NA	22.7	8.3
			Propane	0.158	583	30.0	50.0	2.4	1.9	4.4	-9.4	3.0	10.6	1.2	9.9	20.3	-7.1
Murata & Hashizume [46]	10.3	Copper	R-113	0.031	517	12.9	2.2	1.3	2.2	1.05	10	8.4	18.8	41.4	23.6	24.6	9.2
			R-114	0.061	699	22.1	36.6	2.9	36.6	1.91	7.6	18.8	41.4	23.6	21.4	-9.2	
Hambreus [33]	12.0	Copper (elect.)	R-123	0.0546	300	30.0	20.0	4.1	0.08	0.39	3	13.0	9.1	14.1	9.2	18.6	27.7
			R-134a	0.049	137	6.0	30.0	2.1	0.17	0.09	0.09	26	13.0	14.0	11.1	NA	16.1
Chaddock & Buzzard [27]	7.7	Copper (electr.)	R-502	0.0085	45	3.8	20	4.2	0.04	0.008	26	12.3	15.2	16.3	NA	29.4	9.7
			R-502	0.059	358	23.7	70	5.2	0.36	0.567	5.4	6.1	4.7	NA	28.5	3.3	
Kattan et al. [39]	12.0	Copper (liquid)	R-502	0.15	100	8.0	3.0	2.1	0.14	0.049	15	19.0	15.5	26.5	NA	32.7	8.7
			NH ₃	0.044	300	10.0	54.0	6.2	2.61	0.442	-17.1	-7.0	-9.8	NA	-22.2	-7.0	
Steiner & Schlunder [20]	14.0	Copper (elect.)	Nitrogen	0.186	44	0.5	5.0	1.0	0.05	0.031	42	58.6	52.2	44.4	51.4	26.0	46.6
			Nitrogen	0.461	460	34.6	75.0	9.2	2.2	3.3	-58.6	-52.2	-42.1	45.8	-6.8	-44.9	
Mohr & Runge [18]	4.0	Copper (electr.)	Nitrogen	0.0873	154	1.0	10	0.26	0.02	0.35	21	29.3	33.8	29.2	120.2	23.0	29.0
			Neon	0.0564	209	50.0	90	17.4	0.74	0.61	-19.7	-17.5	-16.1	106.1	6.4	-29.0	
Wright & Walters [57]	6.3	Copper (elect.)	Para H ₂	0.0175	78	1.0	13.0	6.0	0.05	0.11	15	48.4	40.4	63.4	52.4	56.8	60.0
			Argon	0.036	125	20.0	70.0	34.7	0.49	0.28	0.028	18	17.6	18.5	27.0	NA	13.2
Muller et al. [23]	14.0	Copper (Elect.)	Argon	0.413	412	10.0	2.6	0.42	1.88	587	18	2.0	11.5	-27.0	NA	-4.3	-46.7
			Argon	0.0134	120	1.8	0.1	0.36	0.05	0.064	4822	33	23.4	38.4	116.2	NA	169.7
All data	1.95 25.0		Argon	0.413	460	97.0	0.9	74.2	1.79	1.35	1086	-0.3	24.5	114.9	NA	164.7	28.5
			Argon	0.0134	10	1.0	0.0	0.26	0.01	0.0008	4822	1086	17.5	18.9	26.0	27.8	36.8
				0.413	1382	788	95.0	74.2	1000			-6.4	-4.9	+6.6	+9.8	-7.5	

* Reported heat transfer coefficients are mean for the tube length. All other data are local heat transfer coefficients

Table 2: Results of comparison of data for vertical tubes and annuli with various correlations

Data of	Dia. mm	Material (Heating by)	Fluid	P _r	G Kg/m ² s	q kW/m ²	x, %	Bo x 10 ³	Co	No. of data points	Deviation, %				Mean Average	
											Shah	G-W	L-W	Kandlikar		S-T
Naitoh [48]	16.5	SS (Liquid)	Water	0.783	1250	100	0.0	0.96	0.34	7	8.8	8.0	110.8	15.9	28.8	38.4
Wright [56]	18.2	SS (Electr.)	Water	0.0053	434	99	1.0	0.56	0.15	71	10.1	11.4	14.5	8.7	25.0	12.6
	12.0			0.0078	796	154	11.8	1.5	1.0	0.18	37	1.4	-8.6	11.2	-6.6	23.0
Dengler & Addoms [30]	25.4	Copper (Steam)	Water	0.0068	666	118	1.4	0.52	0.18	37	21.5	24.0	37.1	15.1	43.9	10.8
				0.014	2437	274	10.0	1.07	6.4	21.9	36.8	42.8	0.0			
Piret & Isbin [24]*	27.1	Copper (Electr.)	Water	0.011	721	95	1.7	0.6	0.15	5	11.5	21.3	34.7	13.1	40.1	12.2
				0.0046	394	19.4	0.19	0.22	1.27	4	9.7	40.9	88.3	10.2	53.4	6.4
Adorni et al [25]	3.2	SS (Electr.)	Water	0.022	347	5.9	0.64	0.29	1.17	4	9.1	13.5	80.8	NA	26.9	5.6
				0.0204	943	55.3	2.4	0.99	3.43	4	7.8	3.7	47.9	NA	26.9	0.2
Morozov [44]	13.8	SS (Electr.)	water	0.011	681	10.8	0.26	0.29	1.02	4	6.5	7.8	90.7	NA	10.3	12.9
				0.32	779	85.7	1.6	1.8	4.43	39	-6.5	7.8	90.7	NA	8.0	-12.9
Robertson & Wadekar [51]	10.0	Copper (Electr.)	Ethanol	0.32	980	420	14.0	0.66	0.18	38	22.2	15.0	15.4	24.5	29.3	32.2
				0.32	3000	1250	69.6	5.9	1.68	4	-14.7	-4.2	-5.5	-15.2	-22.2	-27.4
Staub & Zuber [53]	10.0	Copper (Electr.)	R-22	0.228	6085	261	0.0	0.24	0.55	6	20.9	28.6	16.7	30.5	58.5	35.9
				0.0244	145	25.5	3.0	2.1	0.05	51	4.4	25.5	9.6	-17.5	32.0	11.8
Lazarek & Black [42]	3.15	SS (Electr.)	R-113	0.121	11071	375	20.0	0.26	1000	8	21.3	17.7	23.3	NA	20.6	9.4
				0.477	290	104.	56.0	7.0	0.90	38	-21.3	-17.7	23.3	NA	-19.6	-6.6
Johannes [35]	2.1	Monel (Electr.)	Helium	0.121	153	12.1	4.0	3.95	0.41	8	40.0	33.8	34.8	33.5	57.5	45.2
				0.57	896	70.7	21.0	3.98	1.12	10	-40.0	-33.8	-34.8	33.4	-57.7	-45.2
Keilin [40]	2.0	Copper (Electr.)	Helium	0.477	502	64.0	4.0	16.1	0.06	7	10.4	32.5	23.1	38.2	54.5	24.4
				0.68	130	0.5	3.2	2.0	0.92	15	5.4	32.5	-23.1	37.6	-54.5	-24.4
Ogata & Sato [17]	1.1	SS (Electr.)	Helium	0.477	28	0.1	1.3	0.9	0.49	14	27.2	35.6	35.1	NA	25.9	51.5
				0.477	96	3.0	39.4	40.3	11.0	19.2	31.6	41.1	24.8	NA	-25.9	-51.5
				0.477	87	0.2	2.0	0.9	0.53	14	28.5	41.1	24.8	19.5	39.7	
				0.477	87	1.4	40.0	8.1	8.62	14	9.5	12.3	15.1	NA	-13.5	-39.7
				0.477	87	1.4	40.0	8.1	8.62	14	11.2	9.1	-14.1	14.7	29.5	
				0.477	87	1.4	40.0	8.1	8.62	14	-5.5	9.1	-14.1	11.3	-29.4	

Data of	Dia. mm	Material (Heating by)	Fluid	Pr	G Kg/m ³ s	q kW/m ²	x, %	Bo x 10 ⁴	Co	No. of data points	Deviation, %					Mean Average		Chen-Cooper						
											Shah	G-W	L-W	Kandlikar	S-T	L-W	Kandlikar							
Pappel & Hendricks [19]	2.0	SS (Electr)	Nitrogen	0.64	2210	212	0.00	9.2	1000	1	0.10	19.6	14.3	436.3	12.5	52.0	-0.10	19.6	-14.3	436.3	12.5	-52.5		
																							13.9	6.8
Klimenko & Sudar-chikov [22]	9.0	SS (Electr.)	Nitrogen	0.14 0.26	220	9.0	2.0	2.35	0.09	20	-3.7	19.7	16.1	269.8	31.3	-7.2	-3.7	6.8	7.8	269.8	31.3	-7.2	-7.2	
																								18.6
Talty [15]	19	Brass (Liquid)	Heptane	0.037	231 454	7.7 31.7	0.14 8.1	0.99 1.73	0.53 6.9	33	18.6	18.6	19.7	NA	13.6	27	0.8	8.9	17.4	NA	13.6	-9.1	-27	-27
	25.3				266 391	13.6 35.6	0.20 5.00	0.69 1.59	0.77 3.98	28	16.9	10.5	17.1	NA	18.9	34.3	-15.5	-6.8	7.9	NA	-16.1	34.3	34.3	34.3
	19.0		Pentane	0.030	251 408	9.1 22.9	0.28 8.3	0.85 2.16	0.48 16.6	51	13.1	11.4	24.5	NA	12.2	20.5	-0.9	9.1	24.0	NA	-1.8	-20.0	-20.0	-20.0
	25.3				266 399	13.6 38.4	0.61 11.7	1.11 3.74	0.35 16.7	54	11.3	5.4	10.9	NA	17.4	36.4	-10.6	-2.1	7.5	NA	-16.5	-36.4	-36.4	-36.4
	19.0		Methanol	0.0156	280 459	26.2 49.7	0.12 4.3	0.85 1.40	0.48 7.3	22	25.9	16.7	38.8	NA	18.7	13.3	-25.9	-16.7	38.8	NA	-17.0	-1.4	-1.4	-1.4
	25.3				314 553	20.3 53.5	0.19 4.3	0.60 1.09	0.65 5.5	54	35.2	21.9	33.6	NA	12.1	22.2	-35.2	-21.9	33.6	NA	-10.7	-22.2	-22.2	-22.2
	25.4		Cyclohexane	0.025	335 488	10.1 41.6	0.5 10.0	0.58 3.02	0.37 4.46	52	15.9	6.8	24.0	NA	16.8	26.0	-15.9	-6.4	24.0	NA	-15.6	-26.0	-26.0	-26.0
	19.0				390 482	7.9 24.1	0.36 6.1	0.46 1.86	0.57 5.71	23	8.9	9.8	51.4	NA	15.4	9.6	-5.2	9.1	51.4	NA	6.0	-9.2	-9.2	-9.2
	25.4		Benzene	.0203	347 600	12.7 41.4	0.20 8.5	0.59 2.58	0.39 8.4	55	13.7	9.3	24.7	NA	9.9	28.0	-11.2	-0.3	24.6	NA	-3.6	-28.0	-28.0	-28.0
	19.0				293 521	16.5 43.1	0.26 8.7	1.34 2.75	0.4 6.8	48	11.7	8.2	17.2	NA	16.6	22.0	-5.9	1.2	16.8	NA	-16.3	-21.3	-21.3	-21.3
All data	1.1 27.1				28 11071	0.2 1250	0.00 70.1	0.22 40.3	0.09 1000	773	17.6	14.9	25.2	47.4	20.4	22.7	-9.2	+20.5	25.2	47.4	20.4	22.7	22.7	22.7

a. annulus, 8.2/5.0 OD/ID, bilateral heating, data for outer tube
b. annulus, 8.2/5.0 OD/ID, bilateral heating, data for inner tube
c. annulus, 8.2/5.0 OD/ID, heating on inner tube only
d. annulus, 20.0/14.2 OD/ID. Inner tube heated

Table 3: Summary of results for horizontal & vertical channels

Correlation of	Mean Dev. %	
	a	b
Shah	17.5	17.3
Gungor & Winterton	17.3	18.6
Chen-Cooper	23.2	22.4
Liu & Winterton	25.7	37.5
Steiner & Taborek	30.0	36.5
Kandlikar	32.2 c	46.0

- giving equal weight to each data point
- giving equal weight to each data set
- 16.8 % if the data for neon, N₂, & R-22 are deleted.

Table 4: Complete range of data satisfactorily predicted by the correlation of Shah [8]

Parameter	Range of data
Fluids	water, R-11, R-12, R-22, R-32, R-113, R-114, R-123, R-134a, R-152a, R-502, ammonia, propane, isobutane, carbon tetrachloride, isopropyl alcohol, ethanol, methanol, n-butanol, cyclohexane, benzene, heptane, pentane, nitrogen, argon, hydrogen, nitrogen, and helium
Test channels	Tubes and annuli (heated on inside, outside, and bilateral). Horizontal and vertical
Heating method	Electric, steam, liquid
Diameter, mm	1.1 to 27.1
Reduced pressure	0.0053 to 0.78
G, kg/m ² s	10 to 11,071
q, kW/m ²	0.2 to 1,250
x, percent	0 to 95
Box10 ⁴	0.22 to 74.2

APPENDIX

The Shah Correlation

The Shah correlation is given by the following equations:

$$h_{TP} = 230Bo^{0.5}h_{LO} \quad (A1)$$

$$h_{TP} = 1.8 \left[Co(0.38Fr_L^{-0.3})^n \right]^{0.8} h_{LO} \quad (A2)$$

$$h_{TP} = FBo^{0.5} \exp \left[2.47 \left(Co(0.38Fr_L^{-0.3})^n \right)^{-0.15} \right] h_{LO} \quad (A3)$$

$$h_{TP} = FBo^{0.5} \exp \left[2.74 \left(Co(0.38Fr_L^{-0.3})^n \right)^{-0.1} \right] h_{LO} \quad (A4)$$

$$h_{TP} = h_{LT} \quad (A5)$$

The predicted h_{TP} is the largest of the values given by the above equations. $n = 0$ for horizontal tubes with $Fr_L > 0.04$ and for vertical tubes at all values of Fr_L , $n = 1$ for horizontal tubes with $Fr_L < 0.04$. $F = 14.7$ for $Bo > 0.0011$, else $F = 15.43$. The above equations are the same as in the published Shah correlation (1982) but have been rearranged for ease of computer programming.